

# Constraint Programming: ECL<sup>i</sup>PS<sup>e</sup>

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# Objectives

- first steps in ECL<sup>i</sup>PS<sup>e</sup>
- generic and basic framework for constraint programming
- some constraint predicates and solvers
- illustration with examples

# Generic framework

# A very useful command of ECL<sup>i</sup>PS<sup>e</sup>

## help

- `help text.` : list all matching predicates
- `help(text).` : list all matching predicates
- `help(predicate/arity)` : help on predicate of arity ar
- `help(module:predicate/arity)` : help on predicate of arity ar from the module/library module

# Basic framework

a constraint program :

1. variable and domain declaration
2. setting constraints
3. search

in ECL<sup>i</sup>PS<sup>e</sup> :

```
1 :-lib(fd).                                % load fd constraints/solver
2 problem(Vars) :-
3   domainVars(Vars),                      % associate domains to variables
4   setConstraints(Vars),                  % setting constraints
5   search(Vars).                         % often labeling
```

# Domain declaration

finite domains :

1. as sets :  $x :: [1, 3, 6]$
2. as interval (but used as sets) :  $x :: [1..300]$
3. as sets of atoms :  $x :: [\text{blue}, \text{ red}, \text{ green}]$
4. for a list of variables :  $[x, y, z] :: [0, 1]$

# Domain declaration : example

```
1 send(L) :-  
2     L=[S,E,N,D,M,O,R,Y],  
3     [E,N,D,O,R,Y] :: [0..9],  
4     [S,M] :: [1..9],  
  
1 [eclipse 17]: send1(L).  
2  
3 L = [S{[1..9]}, E{[0..9]}, N{[0..9]}, D{[0..9]},  
4     M{[1..9]}, O{[0..9]}, R{[0..9]}, Y{[0..9]}]  
5 Yes (0.00s cpu)
```

# FD constraints

finite domain constraints :

1. equality constraints :  $?X \#= ?Y$
2. disequality constraint :  $?X \#\backslash= ?Y$  or  $?X \#\# ?Y$
3. greater than constraint :  $?X \#> ?Y$
4. less than constraint :  $?X \#< ?Y$
5. greater than or equal constraint :  $?X \#>= ?Y$
6. less than or equal constraint :  $?X \#<= ?Y$
7. all different constraint : `alldiff(ListVars)`

# FD constraints : example (ctd)

program :

```
1 send(L) :-  
2     L=[S,E,N,D,M,O,R,Y],  
3  
4     % domain declarations  
5     [E,N,D,O,R,Y] :: [0..9],  
6     [S,M] :: [1..9],  
7  
8     % constraints  
9     1000*S + 100*E + 10*N + D  
10    +1000*M + 100*O + 10*R + E  
11    #= 10000*M + 1000*O + 100*N + 10*E + Y,  
12    alldifferent(L).
```

# FD constraints : example (ctd)

answer :

```
1 [eclipse 25]: send2(L).
2 L = [9, E{[4..7]}, N{[5..8]}, D{[2..8]}, 1, 0, R{[2..8]}, Y{[2..8]}]
3
4 There are 11 delayed goals. Do you want to see them? (y/n)
5 Delayed goals:
6      E{[4..7]} #~ N{[5..8]}
7      E{[4..7]} #~ D{[2..8]}
8      E{[4..7]} #~ R{[2..8]}
9      E{[4..7]} #~ Y{[2..8]}
10     N{[5..8]} #~ D{[2..8]}
11     N{[5..8]} #~ R{[2..8]}
12     N{[5..8]} #~ Y{[2..8]}
13     D{[2..8]} #~ R{[2..8]}
14     D{[2..8]} #~ Y{[2..8]}
15     0 - Y{[2..8]} + 91 * E{[4..7]} - 90 * N{[5..8]}
16             + 10 * R{[2..8]} + D{[2..8]}#=0
17     R{[2..8]} #~ Y{[2..8]}
18 Yes (0.00s cpu)
```

# Search : labeling

- labeling = enumeration
- labeling : instantiates all variables in a list to values in their domain (get next value by backtracking)
- defined as :

```
1      labeling([]) .  
2      labeling([Var|Rest]) :-  
3          indomain(Var),  
4          labeling(Rest) .
```

# Search : labeling (2)

labeling can be improved

strategies to select the variable :

- `deleteff(Var,List,Rest)` : to select the variable with smallest domain
- `deleteffc(Var,List,Rest)` : to select the variable with smallest domain and most constrained

strategies to select the value :

- `mindom` : to select the minimum value
- `maxdom` : to select the maximum value

# Labeling : example (ctd)

program :

```
1 send(L) :-  
2     L=[S,E,N,D,M,O,R,Y],  
3  
4     % domain declarations  
5     [E,N,D,O,R,Y] :: [0..9],  
6     [S,M] :: [1..9],  
7  
8     % constraints  
9     1000*S + 100*E + 10*N + D  
10    +1000*M + 100*O + 10*R + E  
11    #= 10000*M + 1000*O + 100*N + 10*E + Y,  
12    alldifferent(L),  
13  
14    % enumeration  
15    labeling(L).
```

# Labeling : example (ctd)

answer :

```
1 [eclipse 44] : send3(L).  
2  
3 L = [9, 5, 6, 7, 1, 0, 8, 2]  
4 More (0.00s cpu) ? ;  
5  
6 No (0.00s cpu)
```